# Temporal dynamics in bistable perception 

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#### Abstract

Bistable perception is fundamentally a dynamic process: Our perceptual experience continuously alternates when an ambiguous or rivalrous stimulus is observed. Here we present a method to analyze instantaneous measures of dominance and transition between percepts. The analysis extracts three time-varying probabilities. First, the transient preference represents the probability of perceiving one interpretation at one instant. Second, the reversal probability is the probability that the current percept will change at the next evaluation. Finally, the survival probabilities are the probability that at one instant the current percept will not switch to the alternative interpretation. We derive the relationships between these probabilities and offer a test of independence between consecutive percepts. We also introduce a simple technique to sample the observer's perception at regular intervals. The analyzing method is illustrated with the example of binocular rivalry. We demonstrate Levelt's second proposition with the survival probability measure and show that the consecutive rivalrous percepts are not independent.


Keywords: bistability, perceptual dynamics, ambiguous perception, binocular rivalry, Levelt's second proposition

## Introduction

Bistable perception arises when a stimulus can be interpreted in two distinct ways. Two experimental situations have been specifically designed to produce bistable perception. First, the stimulus can be such that it does not contain enough information to lead to a unique interpretation. Examples of such ambiguous stimuli are the Necker cube (Necker, 1832; Attneave, 1971) and other threedimensional objects (e.g., Mamassian \& Landy, 1998, 2001). The second experimental situation occurs when the stimulus contains conflicting information about the plausible interpretations. Examples of such rivalrous stimuli include those presented during binocular rivalry (e.g., Wade, 1975a; Tong, 2001; Blake \& Logothetis, 2002) and those where depth cues are in conflict (van Ee, Adams, \& Mamassian, 2003).

A full explanation of bistable perception involves an understanding of why one of the percepts is perceived first and why percepts alternate at a particular rate when the stimulus is continuously presented for a long time. These two aspects of bistability are most likely intertwined: The stronger a percept is, the more likely it will be perceived first and perceived more often once the percepts start to alternate. Therefore, the mechanisms responsible for the selection of the first percept and the rate of reversal to the other are likely to involve common structures, although this has yet to be demonstrated empirically.

The tools used to measure ambiguous and rivalrous perception are however still rudimentary. Most measures are based on the concept of the phase duration, which is the length of time during which one percept is sustained.

In his influential monograph on binocular rivalry, Levelt (1965) uses the mean dominance duration (the mean of the phase durations), the relative predominance (percentage of the total viewing time that one percept is reported), and the alternation rate. A more detailed picture is obtained by reporting the whole distribution of phase durations. Like most time distributions (Leopold \& Logothetis, 1999), this distribution is positively skewed, that is, short durations are more frequent than long ones (see Figure 2 below). There are thus several valid probability distribution functions that can be used to fit the distribution of phase durations ( De Marco et al., 1977), among which the most popular are the gamma (e.g., Levelt, 1967) and log-normal (e.g., Lehky, 1995) distributions. Best-fitting parameters are then used to summarize the data.

Phase durations provide an important description of bistable perception. Short phases are an indication of an unstable system, and thus the search for the conditions that affect perceptual stability benefits from the analysis of phase durations or alternation rates (e.g., Blake, Sobel, \& Gilroy, 2003). There are however two issues with focusing on phase durations to study bistable perception.

First, the distribution of phase durations does not really represent the dynamics of bistability because the times at which the durations were recorded are not taken into account. Even if consecutive phase durations are uncorrelated (e.g., Fox \& Hermann, 1967), the distribution cannot capture slow variations in the rate of reversals (see discussion on stationarity below). It is therefore appropriate to look for an alternative measure that preserves the order of events.

The second issue arises once the distribution is fitted with a gamma or other distribution. Surprisingly, these parameters are often left completely uninterpreted. One consistent finding, though, is that the two parameters of the gamma distribution ( $\lambda$ and $r$; see Figure 2) are strongly correlated (Borsellino et al., 1972; De Marco et al., 1977) and often identical. While the reason for this correlation is still not clear, it does indicate that the gamma distribution has one degree of freedom too many.

In this study, we propose a simple method to record and analyze bistable data. We argue that the analyzing method satisfactorily addresses the two concerns highlighted above. Even though the analysis is relatively independent of the way the data have been obtained, we also present a straightforward way to record the observer's percept at regular intervals.

The usual approach in studying bistable perception is to ask observers to press one of two keys whenever their percept changes. With this method, there is a potential danger of contamination of the perceptual data with the motor responses. For instance, the observers could reevaluate the stimulus whenever they press a key to reassure themselves that their response really matches their percept, and this in turn might accelerate the reversal rate. On the contrary, observers could momentarily release their attentional focus, and potentially slow down their reversal rate. One way to avoid the contamination of bistable perception with motor responses, including eye movements and blinks, is to use afterimages (Wade, 1974, 1975b). However, this method is not appropriate if one is interested in the changing percept with time. We propose here an alternative way to record the observer's time-varying percepts.

In short, the method is as follows. Observers are presented with an ambiguous stimulus and are prompted to report their percept repeatedly at the sound of an auditory beep. The beeps are separated by an average of 2 s with a random temporal jitter to preclude anticipation. Several runs are recorded in this way for each experimental condition. The analysis then consists of computing a survival probability, namely the probability that one percept for one beep time survives onto the next beep. This survival probability is computed for the whole duration of the run, thereby providing an instantaneous representation of the perceptual dynamics. Two main aspects can then be extracted from this survival probability: a time constant reflecting the time to reach a stationary regime, and an asymptotic value reflecting the mean survival probability in the stationary regime.

Next we provide the details of the method and apply it to a classical case of binocular rivalry. In particular, we describe how the method can be used to test Levelt's second proposition. We conclude with a discussion of the merits of our method over the more traditional approach of reporting the parameters of the gamma distribution.

## Experiment 1: The technique

We present our technique for studying the temporal dynamics of bistable perception with the help of a binocular rivalrous stimulus. Because this stimulus is very common (for a review, see Blake, 1989), it will be easy to compare our technique with more conventional approaches. We use this example to define the concepts of transient preference, reversal probability, and survival probabilities. To track the temporal effects of an initial perceptual bias, we impose a large contrast difference between the two eye's images.

## Methods

## Participants

Two undergraduate students (one male, one female) from the University of Glasgow took part in this experiment. They were naive about the purpose of the experiment, gave their consent before running the experiment, and were paid for their participation. Both observers had normal visual acuity in both eyes.

## Stimuli

Stimuli were Gabor patches (sine wave gratings modulated by a Gaussian envelope) oriented at $\pm 45$ deg relative to the vertical (Figure 1A). The orientation of the Gabors was randomized from one trial run to the next with the constraint that the orientation in one eye was always orthogonal to that in the other eye. The size of the Gabor was kept small to minimize fused or piecemeal percepts where


Figure 1. General methods. (A). Example of a binocular rivalry stimulus used in this study. (B). Time course of a run of trials. Once the visual stimulus is on, an auditory beep is presented at intervals of approximately 2 s . Observers have to report their current interpretation (here, Left or Right orientation) at the time of the beeps.
the interpretation is a mixture of the left and right images. The size (at half-height of the Gaussian envelope) was 0.83 deg of visual angle in diameter. The spatial frequency of the grating was set to 2.5 cycles $/ \mathrm{deg}$. The contrast ratio between the left and right eye images was fixed to $25 \%$. Which eye saw the full-contrast Gabor and which eye saw the $25 \%$-contrast Gabor was randomized between trials. In the analyses below, we combine trials according to the stimulus contrast, so we present our results relative to either the high-contrast or low-contrast stimulus rather than left or right eye.

The stimuli were surrounded by a frame composed of small squares, half of them black, the others white. This frame was non-rivalrous (same contrast in both eyes) and had zero disparity.

Stimuli were presented on a split-screen Wheatstone stereoscope where the display was a 21 -in Sony Trinitron CRT monitor driven by an Apple PowerMac computer. The experiment was controlled by a program that ran under Matlab using the PsychToolbox functions (Brainard, 1997; Pelli, 1997). The experiment was run in a dark room and the observers had to place their heads in a chin- and head-rest to minimize head movements. The viewing distance was 80 cm .

## Procedure

Observers were repeatedly prompted to report the perceived orientation of the Gabor at the sound of an auditory beep (Figure 1B). Beeps were presented on average every 2 s , starting 1 s after the stimulus onset. A small temporal jitter was introduced to reduce anticipatory responses. This jitter was drawn from a uniform distribution extending 500 ms before and after the planned mean time occurrence of the beeps. In practice, the first beep could therefore occur anytime between 0.5 s and 1.5 s after stimulus onset, the next beep anytime between 2.5 s and 3.5 s , and so on.

Observers had to press one of two keys with their left or right index fingers, reporting their percept at the time of the beep. If uncertain, they were asked to choose the percept that appeared the strongest. Responses made more than 1 s after the beep were discarded. This strict constraint allowed us to ascertain that a response did not interact with the next beep. To minimize the probability of missing the first beep, a count-down from 5 s before the stimulus onset was displayed on the monitor. The zero-disparity frame was also presented during this count-down to help stabilize vergence before stimulus onset.

In this first experiment, the presentation duration of a run (the time when the Gabors were shown) was set to 50 s . Each observer ran 100 such runs ( 50 at each contrast ratio balanced across the two eyes) with a short break between consecutive runs.

## Results

The results are split in phase durations, transient preference, reversal probability, and survival probabilities.

## Phase durations

The traditional way to analyze data from bistable experiments is to report the distribution of the phase durations. Phase durations of each dominant percept (here the orientation of the high- and low-contrast Gabors) can be computed by counting the consecutive number of times that a given percept is reported to be identical. For instance, if the same orientation is perceived for three consecutive beeps before the percept reverses to the other orientation, this particular phase will be assigned a duration of 6 s (3 times the inter-beep interval of 2 s ).

It is clear that the phase durations we have recorded are affected by the inter-beep interval. We missed phase durations shorter than 2 s , but also slightly exaggerated all phase durations (by combining two phases that were separated by a missed phase). More discussions of this issue can be found in Appendix D.

Figure 2 illustrates the distribution of phase durations for the high-contrast percepts for the two observers (the low-contrast percepts had similar distributions but fewer


Figure 2. Phase-duration analysis for the two observers in Experiment 1. The distributions of phase durations are well fit by a two-parameter ( $\lambda, r$ ) gamma distribution of the form $g(x)=\left[\lambda^{r} x^{r-1} / \Gamma(r)\right] \exp (-\lambda x)$, where $\Gamma$ is the gamma function. The phase durations have been normalized to their respective means ( $\mu$ ) before the fitting procedure was applied.
bins). In these plots, the phase durations have been normalized relative to their respective means ( $\mu=9.15 \mathrm{~s}$ and 7.60 s for observers DM and KM, respectively). The distribution of these phase durations follows a sharp rise and a slow fall that is well summarized by a gamma distribution (Levelt, 1965). The best-fitted parameters for the gamma distribution fall between 2 and 3, and this is consistent with numerous previous studies (for references, see Blake \& Logothetis, 2002). From this analysis of the phase durations, it seems therefore that our method of recording the dynamics of binocular rivalry did not substantially affect the pattern of responses.

## Transient preference

What the phase-duration analysis fails to capture, however, is the time course of the percepts. A natural depiction of this time course is provided by the transient preference. The transient preference is simply the proportion of percepts consistent with one of the two interpretations, here arbitrarily chosen as the high-contrast Gabor. This proportion is computed by taking the average of the percepts across all runs, separately for each beep time.

Not surprisingly, both observers show an initial strong bias for reporting the orientation of the high-contrast image. The initial bias is in fact so consistent with the highcontrast image that the transient probability is not significantly different from 1 at the first beep. Interestingly though, this initial bias gradually wears off and the transient preference reaches a stable regime (Figure 3).

To summarize the dynamics of transient preferences, we fit the data with a scaled cumulative Gaussian with 3 degrees of freedom (see Appendix A). The first degree of freedom $\alpha$ is the asymptotic value of the stationary regime. The second degree of freedom $\tau$ is the time constant to reach the stable regime. Finally, the third degree of freedom $\sigma$ is the slope of the function at its inflexion point. We define the time constant as the time at the intersection of the asymptotic line and the tangent at the inflexion point (see Figure 3 and Appendix A).

Both observers show similar asymptotic values in the stationary regime $(\alpha=0.709$ and 0.708 for observers DM and KM, respectively). In spite of this similarity, the observers took different amounts of time to reach these stationary regimes ( $\tau=21.5 \mathrm{~s}$ and 7.3 s , respectively). This fundamental difference in temporal dynamics between observers was not readily visible in the phase-duration analysis.

## Reversal probability

While the transient preference is a good description of the current percept, it is not a measure of the stability of that percept. We define the reversal probability as the probability that the current percept will change at the next beep, irrespective of the current percept. The reversal probability therefore reflects how fast percepts change. If we let


Figure 3. Transient preference for the two observers in Experiment 1. The transient preference is the proportion of responses corresponding to the high-contrast image for each beep occurrence. There is a strong initial bias for the high-contrast image, but this bias wears off after several seconds for both observers. The procedure used to estimate the time constant $\tau$ of this process is illustrated in red on the top graph. Error bars indicate standard error of the means.
$v$ represent the reversal probability and $u$ the alternation rate (in number of changes per second), then

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\begin{equation*}
u=v / \delta, \tag{1}
\end{equation*}
$$

where $\delta$ is the mean inter-beep interval (here 2 s ). In other words, the higher the reversal probability, the faster the alternation rate. We should note that in this equation, $v \leq 1$ because it is a probability. If the reversal probability is too close to 1 for comfort, the experimenter should attempt to reduce the inter-beep interval or avoid the use of the discrete sampling technique. As a conservative rule, we suggest that caution is exercised if $v>0.5$.

Similarly to the analysis of the transient preference, the reversal probability is strongly biased at first and gradually reaches a stable regime (Figure 4). The initial bias is in favor of a slow alternation rate, so much so that for our stimulus, the initial reversal probability is not significantly different from zero. We fit these data with a scaled cumulative Gaussian, again with 3 degrees of freedom (see Appendix A). The first degree of freedom is the asymptotic value of the stationary regime and is very similar between observers ( $\alpha=0.373$ and 0.366 for observers DM and KM, respectively). The second degree of freedom is the time constant to reach the stable regime and is defined as for the transient preference (i.e., the intersection of the asymptotic line and the tangent at the inflexion point). The third degree of freedom is the slope of the function at its inflexion point and is positive for both observers, indicating that the alternation rate progressively increases within a run of trials.

We shall use the reversal probability as a measure of stationarity: When the reversal probability is stable over time, we can say that the alternation of percepts has reached its stationary regime. The fitted time constants $\tau$ are very different between the two observers, observer DM being much slower to reach a stationary regime than KM ( $\tau=19.5 \mathrm{~s}$ and 5.3 s , respectively). The start of the stationary regime can be defined as time $(\tau+\delta)$ where the added $\delta$ reflects the fact that reversal probability refers to the predicted percept at the next beep. These values ( 21.5 s and 7.3 s , respectively) match very well the time constants found for the transient preference. Note however that there is no particular relationship between the transient preference and the reversal probability (for details, see Appendix B). In particular, if the two percepts were matched in strength, we would expect a balanced transient preference from the start of the run (i.e., 0.5 ), and yet we may still observe a reversal probability resembling the one found here. It is for this reason that we define the duration of the nonstationary regime from the reversal probability and not simply from the transient preference.

## Survival probabilities

The transient preference and reversal probability describe the time course of the current percept and the stability of that percept. Another way to represent this information is to use the survival probabilities. The survival probability is the likelihood that the next percept will be identical to the current one. It is defined as a conditional probability on the current percept (see Appendices B and C for its precise definition). There are therefore two distinct survival probabilities, depending on whether the current percept is that of the high- or low-contrast image.

Survival probabilities for our two observers are shown in Figure 5. There are two curves for each observer, one corresponding to the percept linked to the high-contrast stimulus (in filled blue symbols) and the other to the lowcontrast stimulus (in open red symbols). The larger error bars for the low-contrast percepts simply reflect the fact that there were fewer measurements available to estimate these


Figure 4. Reversal probability for the two observers in Experiment 1. The reversal probability is the probability that the current percept will change at the next beep. From the time constant of the fitted function, we can isolate the initial nonstationary regime (on the left side of the dashed vertical line).
probabilities. As with the previous two analyses, the survival probabilities were fitted with scaled cumulative Gaussian functions (Appendix A). We focus our attention on the asymptotic values of the best fits.

For both observers, the survival probability of the highcontrast percept is larger than the one for the low-contrast percept. In other words, if the high-contrast stimulus is the one perceived at one instant, it has a larger probability to survive to the next beep than if it were the low-contrast stimulus. This result was to be expected because we already saw that the high-contrast stimulus was chosen more often (Figure 3). The analysis of the survival probabilities allows us to split the contribution of each stimulus to the highcontrast dominance. Asymptotic values for the highcontrast percept were $\alpha_{H}=0.740$ and 0.744 for observers DM and KM, respectively, compared to the asymptotic values for the low-contrast percept $\alpha_{L}=0.369$ and 0.393, respectively.

The survival probabilities are transient measures of dominance: The higher the survival probability of one per-


Figure 5. Survival probabilities for the two observers in Experiment 1. The survival probability is the conditional probability that the next percept will be identical to the current one. The two different percepts here are the orientation corresponding to the high-contrast stimulus ( $H$, in blue) and the orientation of the low-contrast stimulus ( $L$, in red). Error bars were used for the maximum likelihood fit and are proportional to the inverse of the square root of the number of samples (large error bars indicate a small number of samples).
cept, the more likely this percept will be sustained and the less likely the other percept will arise. There is therefore a direct relationship between the transient preference and the survival probabilities (see Appendix B). Similarly, the reversal probability can also be expressed as a function of the survival probabilities (see again Appendix B).

Because both the transient preference and the reversal probability can be expressed as a function of the survival probabilities, these latter two are sufficient to describe the temporal dynamics of bistability by themselves. Note that this description is valid here only to the first order (that is, how the current state will affect the next state). Higher order survival probabilities can be defined with a history going back a few beeps. For instance, a second-order description would be obtained by measuring how the next state
depends on the current and previous states. These higher order descriptions are beyond the scope of this study (e.g., see Maloney, Dal Martello, Sahm, \& Spillmann, 2005).

## Experiment 2: Stationarity

The first experiment allowed us to define our procedure to measure and analyze bistable perceptions. In a second experiment, we test the robustness of the technique on a larger population of observers. In addition, we extend the duration of the runs six-fold to ensure that beyond the critical time constant, the regime of alternations is indeed stationary.

## Methods

## Participants

Seventeen undergraduate students from the University of Glasgow took part in this experiment. Six more ran the experiment but were later discarded because they missed too many responses (see Procedure below). All were naïve to the purpose of the experiment, gave their written consent, and were paid for their participation. The observers had normal or corrected-to-normal visual acuity in both eyes.

## Stimuli

Stimuli were the binocular rivalrous Gabors used in Experiment 1. The contrast of the left and right eye images were set to $100 \%$ and $25 \%$, respectively.

## Procedure

Observers were repeatedly prompted to report the perceived orientation of the Gabor at the sound of an auditory beep. Responses made more than 1 s after the beep were discarded. If an observer missed more than $25 \%$ of the total number of responses, he or she was discarded. While this threshold may appear large, one has to remember that this experiment involved naïve participants who were not particularly thrilled to look at rivalrous Gabors in a dark room for an hour. Experienced observers have almost no missed responses (see previous experiment).

In this second experiment, the presentation duration of a run (the time the Gabors were shown) was extended to 5 min . Each observer ran eight such runs with a short break between consecutive runs.

## Results

## Transient preference

The transient preference for the high-contrast stimulus is shown in Figure 6. Similarly to Experiment 1, there is a strong initial bias that wears off after about 6 s . The mean preference in the stationary regime is 0.613 . There is no apparent change in transient preference beyond the critical time constant.


Figure 6. Transient preference for Experiment 2. The plot shows the mean preference across all observers for the high-contrast interpretation. Error bars are standard errors between observers.

## Reversal probability

The reversal probability is shown in Figure 7. It slowly increases before reaching a stationary regime at 0.455 . Contrary to the previous experiment, the initial reversal probability is significantly greater than zero, possibly reflecting the long-lasting effects of a six-fold increase in presentation time. A fit with a scaled cumulative Gaussian allows us to isolate the initial nonstationary regime, which lasts 27 s on average across all observers.

## Survival probabilities

The survival probability for the high-contrast interpretation was consistently larger than that of the low-contrast


Figure 7. Reversal probability for Experiment 2. Once the stationary regime is reached (on average after 27 s ), the reversal probability is constant.


Figure 8. Survival probabilities for Experiment 2. The survival probabilities are shown in red up-triangles and blue downtriangles for the high-contrast and low-contrast stimuli, respectively.
interpretation (Figure 8). Beyond the time constant, the survival probabilities stayed constant. In the stationary regime, the fitted asymptotic values were $\alpha_{H}=0.62$ and $\alpha_{L}=0.42$.

## Independence

The survival probabilities provide a direct test for the independence of consecutive responses. Two consecutive responses are independent if the next percept cannot be predicted from the current one. Interestingly, a condition of independence is that the two survival probabilities sum to 1 (see Appendix C). Figure 9 shows the distribution of survival probabilities across all observers for Experiment 2


Figure 9. Independence test. The survival probabilities for both low- and high-contrast interpretations are plotted against each other for each observer. The green dashed line represents the constraint for two consecutive percepts to be independent.
(once they have reached the stationary regime). The sums of the pairs of survival probabilities for each observer are on average larger than 1 (mean: 1.050; SE across observers: 0.029 ), indicating that consecutive percepts are not independent. This result is seemingly in contradiction with previous reports that have consistently argued for independence (Fox \& Hermann, 1967; Blake, Fox, \& McIntyre, 1971; Walker, 1975; Lehky, 1995). However, it is important to remember that their independence test was on consecutive phase durations rather than consecutive percepts. Our dependence result might reflect the gradual build-up of adaptation to one percept while this percept is surviving, whereas the independence of phase durations suggests that the adaptation is reset whenever a transition occurs.

## Experiment 3: Perceptual biases

The first two experiments have demonstrated the use of the survival probabilities to describe the temporal dynamics of bistable perception. In this third experiment, we look at how the survival probabilities vary with the strength of the competing stimuli. We vary the relative strength of each stimulus by altering the contrast of the stimulus in one or the other eye.

## Methods

## Participants

Twenty-two naive undergraduate students took part in this experiment. Seven of these participants were discarded because they failed to respond quickly enough (see Procedure below). The analysis below was carried out on the 15 remaining participants.

## Stimuli

Stimuli were identical to those used in the previous experiment, except that six contrast conditions were used. The contrast ratios between the right and left eyes were chosen equi-distant on a log-scale: $0.5,0.66,0.87,1.15$, 1.52 , or 2.0 . The first three contrasts were obtained by setting the contrast of the left eye to 1.0 and varying the contrast of the right eye between 0.5 and 0.87 (see legend of Figure 13); the last three contrasts were similarly obtained by exchanging the roles of the left and right eyes.

## Procedure

The procedure was similar to that used in the previous experiment. Observers ran eight consecutive blocks of runs where each block contained one run for each contrast ratio, presented in random order. Observers took a short break between each run and a longer break between each block.

The inter-beep interval was again 2 s on average and participants had to respond within 1 s after each beep. Those participants who missed more than $25 \%$ of the responses were removed from the final analysis.

## Results

## Transient preference

As expected, the higher the contrast of one eye's image, the larger the probability that the interpretation is consistent with that image. This behavior can be readily seen by looking at the transient preference to report seeing the image presented to the right eye (Figure 10). As for the previous experiments, the transient preference was fitted with a scaled cumulative Gaussian.


Figure 10. Time-varying transient preferences for the right-eye image in Experiment 3. Each plot corresponds to a different contrast ratio between the two monocular images (right eye over left eye). Error bars are standard errors between observers.

The transient preference increases (positive slope parameter) if the asymptotic value is less than 0.5 , and decreases (negative slope) if the asymptotic value is more than 0.5 . This relationship between the slope and the asymptote accentuates the effect of contrast for the initial transient preference. While the asymptote changes modestly with contrast, the initial interpretation is dramatically influenced by contrast. To reveal this effect further, we have isolated the very first interpretation (at the first beep) from the subsequent ones. Figure 11A shows how the first response changes with contrast, and separately, how the mean subsequent responses change with contrast. The change in slope of the fitted cumulative Gaussians shows the difference between the very first response and the other responses. In spite of this difference, there is still a very good correlation between the two (Figure 11B). Hupé and Rubin (2003) found a similar exaggerated bias of the first response for bistable motion stimuli.

## Survival probability

The survival probabilities for the left and right eye images cross over as the contrast ratio varies between 0.5 and 2 (Figure 12). As expected, the survival probability is larger


Figure 11. Comparison of mean initial and subsequent responses in Experiment 3. (A). The mean first response (red open symbols) rises quickly with contrast ratio, whereas the mean subsequent responses (filled blue symbols) rise much more slowly with contrast ratio. (B).There is a very good correlation between the mean first response and the subsequent responses (Pearson's correlation, $R=0.79$ ).
for the image that has the higher contrast, and the difference in survival probabilities reduces as the contrast ratio gets close to 1 .

If we restrict ourselves to the stationary regimes, we can plot the asymptotic value of the survival probabilities as a function of the contrast ratio (Figure 13). Values of the contrast ratio between 0.5 and 1.0 were obtained by fixing the contrast of the left eye image to 1.0 and increasing the contrast of the right image between 0.5 and 1.0. We note that in this range of the contrast ratios, the asymptotic value of the left survival probability varies more rapidly than that of the right survival probability (the slope of the line relating survival asymptote to contrast ratio is -0.246 vs. -0.079 for the left and right survival probabilities, respectively). Conversely, in the range of contrast ratios larger than 1.0 , obtained by fixing the contrast of the right eye image, it is the right survival probability that varies faster with contrast ratio (slopes of 0.040 vs. 0.213 for the left and right survival probabilities, respectively). The ratio of the slopes between the most affected and the least affected eyes is close to 4 ( 3.1 and 5.3 for the ranges [0.5, 1] and [1, 2], respectively).

This behavior is in close agreement with Levelt's second proposition (Levelt, 1965, 1966). According to Levelt, an increase of the stimulus strength in one eye does not


Figure 12. Time-varying survival probabilities for Experiment 3. Red up-triangles now refer to the left-eye image, blue downtriangles to the right-eye image. The survival probabilities cross over as the contrast ratio increases over unity.
increase the mean duration of the ipsilateral percept, but instead reduces the mean duration of the contralateral percept. More recent studies have found a weak but significant effect of the mean dominant duration of the ipsilateral eye (Mueller \& Blake, 1989; Bossink, Stalmeier, \& de Weert, 1993). We found here that even though a change of strength of one eye's image does affect the survival probability of that image, this effect is 4 times smaller than the effect on the other eye's image. In other words, an increase in stimulus strength in one eye does not dramatically boost the survival probability of that eye, but instead greatly decreases the survival probability of the other eye.


Figure 13. Effect of contrast on the asymptote of the survival probabilities for Experiment 3. The two horizontal bars below represent the contrast of each eye to produce a given contrast ratio. The survival probabilities approximate Levelt's second proposition: Increasing the contrast of one eye's image mainly decreases the dominance of the other eye.

One final analysis consists in looking at the relationship between the two survival probabilities for different contrast ratios (Figure 14). We again restrict ourselves to the stationary regime. We can see that the sum of the two survival probabilities is always larger than 1 , indicating that two consecutive percepts are never independent. The lack of independence (as indicated by a departure from 1 for the sum of the survival probabilities) seems to increase for more unbalanced stimuli (as the contrast ratio deviates from 1).

## General discussion

In this work, we have presented a procedure for analyzing the temporal dynamics of ambiguous and rivalrous perception. The procedure consists of measuring the timecourse of the survival probability of each interpretation, that is the probability that the current percept will be sustained for a short duration.

We see several advantages in reporting survival probabilities. First, the survival probability is a transient measure of perception and is therefore relevant for the study of the temporal dynamics of bistable perception. Second, it is sufficient to estimate several other characteristics, such as the transient preference (instantaneous probability of seeing one percept) and the reversal probability (instantaneous probability of experiencing a change of percept). Third, it contains critical information about whether the first response is more biased than the subsequent responses and about the duration of the initial nonstationary regime. Fourth, it provides a test of independence for percepts taken at regular intervals.

The report of survival probabilities should provide a finer measure of similarity between two bistable processes. Previous studies that tested whether two conditions had similar temporal dynamic properties had to rely on the mean alternation rate (Andrews \& Purves, 1997; Chen \& He, 2003; van Ee, 2005) or on the gamma distribution (Logothetis, Leopold, \& Sheinberg, 1996; Leopold \& Logothetis, 1999). It will be of interest to compare the asymptotic values and time constants of the survival probabilities in these experiments. While we prefer the procedure described in this work to collect the survival probabilities, it is also possible to estimate these entities from existent experiments that were obtained with the more traditional method of continuous data collection (see Appendix D).

One may question the effect of presenting regular beeps on the dynamics of bistable perception. It is indeed possible that these beeps will influence the subjective state of the observer. However, given that the rate of beeps is identical for all observers and for all conditions, this influence should be constant throughout the course of a trial and across conditions. Consider the result that phase durations are longer at the beginning of the trial than in the middle and end. With the continuous response method, the observer would press a key less often at the beginning of


Figure 14. Relationship between the asymptotic value of the survival probabilities in Experiment 3. The sum of the two survival probabilities (for the left [LE] and right (RE) eyes) is always greater than 1, indicating that two consecutive percepts are not independent.
the trial. In contrast, with the discrete method, the beeps and the responses occur at the same rate throughout the trial. Overall, one could argue that the discrete sampling method constrains the attentional load of the observer. If confirmed to be true in future studies, this would be a serious advantage for the discrete method because different bistable stimuli are affected differently by attention (e.g., Lack, 1978; Meng \& Tong, 2004; van Ee, van Dam, \& Brouwer, 2005). Potentially, the lack of attentional control may also participate in the large inter-subject variability typically reported in bistable experiments (e.g., Carter \& Pettigrew, 2003). More work is clearly needed to compare the continuous and discrete recording methods.

Our analyzing method can also easily be generalized to multistable perception where the observer's percepts alternate between more than two interpretations. In this case, as many survival probabilities should be defined as there are distinct percepts. In addition, transition probabilities should be introduced to test whether some transitions between two percepts are favored over others (as shown by Suzuki \& Grabowecky, 2002). While we can anticipate that the survival probabilities will reach a stationary regime similarly to that found in this study, the transition probabilities might follow very different dynamics.

Another extension of our method is to consider higher order conditional probabilities. We have restricted ourselves to determine how well the next percept can be predicted from the current one (first-order analysis), and it will be interesting to include the knowledge of the previous percept (second order) as well as older percepts. Ultimately, one could look at the probability of a reversal as a function of time since the last reversal, which is sometimes called the "hazard function" (Taylor \& Aldridge, 1974). These analyses should provide strong constraints for plausible models of bistable perception (e.g., Dayan, 1998; Laing \& Chow, 2002; Wilson, 2003).

In summary, we have proposed a technique to measure and analyze some of the fundamental properties of the temporal dynamics of ambiguous and rivalrous perception. We are currently measuring the survival probabilities in a variety of bistable stimuli to compare the similarities across stimuli and tasks.

## Appendix A: Fitting functions

The transient preference, reversal probability, and survival probabilities share a similar time-course. We chose to represent this temporal function by a scaled cumulative Gaussian with 3 degrees of freedom. The 3 degrees of freedom are the asymptotic probability $(\alpha)$ in the stationary regime, the time constant $(\tau)$ to reach that stationary regime, and the slope $(\sigma)$ of the function at the inflection point. The time constant is defined as the intersection of the asymptotic line and the tangent of the function at the inflexion point (see Figure 3). The fitting function comes in two types, depending on whether the function is monotonically increasing (positive $\sigma$ ) or decreasing (negative $\sigma$ ).

Let $G(m, s, t)$ represent the usual cumulative Gaussian distribution with mean $m$ and variance $s^{2}$ at time $t$

$$
\begin{equation*}
G(m, s, t)=\int_{-\infty}^{t} \frac{1}{\sqrt{2 \pi s^{2}}} \exp \left(-(x-m)^{2} / 2 s^{2}\right) d x \tag{2}
\end{equation*}
$$

The scaled cumulative Gaussian fitting function $H$ is then defined as follows. When $\sigma>0$,

$$
\begin{equation*}
H(\alpha, \tau, \sigma, t)=\alpha G\left(\tau-\frac{\alpha}{2 \sigma}, \frac{\alpha}{\sqrt{2 \pi \sigma^{2}}}, t\right) \tag{3}
\end{equation*}
$$

Alternatively, when $\sigma<0$,

$$
\begin{equation*}
H(\alpha, \tau, \sigma, t)=1-(1-\alpha) G\left(\tau+\frac{1-\alpha}{2 \sigma}, \frac{1-\alpha}{\sqrt{2 \pi \sigma^{2}}}, t\right) \tag{4}
\end{equation*}
$$

The function $H$ presents a singularity at $\sigma=0$. By convention, we shall define

$$
\begin{equation*}
H(\alpha, \tau, 0, t)=\alpha \tag{5}
\end{equation*}
$$

The 3 degrees of freedom of the scaled cumulative function $H$ were adjusted to the data with a maximum likelihood procedure that took into account the variability of each data point to estimate the best fit.

## Appendix B: Survival probability

The knowledge of the survival probabilities is sufficient to infer the mean transient preference and the reversal probability. We detail here the relationships between these different entities.

Let $\delta$ be the mean sampling interval (i.e., 2 s in our experiments). Let also $R(t)$ be the event representing the fact
that the right eye's image is perceived at time $t$ [and similarly for the left eye's image $L(t)$ ]. Given that the two eyes' images are the only two possible interpretations, we have

$$
\begin{equation*}
p(R(t))+p(L(t))=1 \tag{6}
\end{equation*}
$$

The survival probability for the right eye's image $s_{R}(t)$ is the probability that a percept $R$ at time $t$ will survive at time $(t+\delta)$. It is therefore defined as the conditional probability

$$
\begin{equation*}
s_{R}(t)=p(R(t+\delta) \mid R(t)) \tag{7}
\end{equation*}
$$

The survival probability of the left eye's image $s_{L}(t)$ is similarly defined. Note that $s_{R}(t)$ and $s_{L}(t)$ do not necessarily sum to one (see Appendix C).

With the knowledge of the survival probabilities, we can estimate the transient preference at the next beep $p(R(t+\delta))$

$$
\begin{align*}
p(R(t+\delta))= & p(R(t+\delta), R(t))+p(R(t+\delta), L(t)) \\
= & p(R(t+\delta) \mid R(t)) p(R(t))+ \\
& p(R(t+\delta) \mid L(t)) p(L(t))  \tag{8}\\
= & s_{R}(t) p(R(t))+\left(1-s_{L}(t)\right)(1-p(R(t)))
\end{align*}
$$

In the stationary regime, we have

$$
\begin{equation*}
p(R(t+\delta))=p(R(t))=p(R) \tag{9}
\end{equation*}
$$

and Equation 8 for the transient preference reduces to

$$
\begin{equation*}
p(R)=\left(1-s_{L}\right) /\left(2-s_{L}-s_{R}\right) \tag{10}
\end{equation*}
$$

This relationship between transient preference and survival probabilities is illustrated in Figure 15.

In a similar way, the probability $v(t)$ that the current percept will reverse at the next beep can be expressed as

$$
\begin{align*}
v(t)= & p(L(t+\delta), R(t))+p(R(t+\delta), L(t)) \\
= & p(L(t+\delta) \mid R(t)) p(R(t))+  \tag{11}\\
& p(R(t+\delta) \mid L(t)) p(L(t)) \\
= & \left(1-s_{R}(t)\right) p(R(t))+\left(1-s_{L}(t)\right)(1-p(R(t)))
\end{align*}
$$

In the stationary regime, we can use the expression we found for the transient preference probability (Equation 10). In doing this, the reversal probability reduces to

$$
\begin{equation*}
v=2\left(1-s_{L}\right)\left(1-s_{R}\right) /\left(2-s_{L}-s_{R}\right) \tag{12}
\end{equation*}
$$

The relationship between the reversal probability and the survival probabilities is illustrated in Figure 16.

A comparison between Figures 15 and 16 makes it clear that there are no simple relationships between the transient preference and the reversal probabilities. In other words, the transient preference and reversal probability


Figure 15. Contour plot of the relationship between the transient preference and the survival probabilities. Each blue line represents the pairs of survival probabilities that are compatible with a given transient preference (indicated by the number on the line). The two red dots represent the two observers in Experiment 1. The green dashed line indicates the independence constraint (see Appendix C).
represent different aspects of the temporal dynamics of bistability, but both of these aspects can be described from the knowledge of the survival probabilities.

## Appendix C: Independence

How independent are consecutive responses? This question can be answered easily thanks to the survival probabilities. We first list all four possible transitions between consecutive responses and their corresponding expressions in terms of survival probabilities:

$$
\left\{\begin{array}{l}
p(R(t+\delta) \mid R(t))=s_{R}(t)  \tag{13}\\
p(L(t+\delta) \mid R(t))=1-s_{R}(t) \\
p(R(t+\delta) \mid L(t))=1-s_{L}(t) \\
p(L(t+\delta) \mid L(t))=s_{L}(t) .
\end{array}\right.
$$

If one percept is independent of the previous one, then these conditional probabilities reduce to

$$
\left\{\begin{array}{l}
p(R(t+\delta))=s_{R}(t)  \tag{14}\\
p(L(t+\delta))=1-s_{R}(t) \\
p(R(t+\delta))=1-s_{L}(t) \\
p(L(t+\delta))=s_{L}(t) .
\end{array}\right.
$$



Figure 16. Contour plot of the relationship between the reversal probability and the survival probabilities. Each blue curve represents the pairs of survival probabilities that are compatible with given reversal probabilities (indicated by the number on the line). The red dots and the green line are identical to that of Figure 15.

From these equations, the following constraint emerges:

$$
\begin{equation*}
s_{R}(t)+s_{L}(t)=1 . \tag{15}
\end{equation*}
$$

This constraint is a necessary and sufficient condition for the percepts to be selected independently of the previous ones. The constraint is depicted as a green dashed line in Figures 15 and 16.

When the percepts are independent, the transient preference and reversal probabilities simplify. In the stationary regime, we can take back Equations 10 and 12 derived in Appendix B to find

$$
\left\{\begin{array}{l}
p(R)=s_{R}  \tag{16}\\
v=2 s_{R}\left(1-s_{R}\right) .
\end{array}\right.
$$

## Appendix D: Continuous data

In this Appendix, we report a simple procedure to reanalyze previous data sets that were collected with the usual method of asking observers to report any change of percept as soon as it occurred. While we prefer our method of data collection, because it allows for a better control of the observer's attention, the following procedure might be helpful to extract survival probabilities of existing data sets.

We ran six observers with the same stimuli as in the first and second experiments (contrast ratio of 0.25 ), presented for 5 min at a time. Observers saw eight such sessions. Instead of responding at regular intervals, observers were given two keys assigned to the two possible interpreta-
tions (left- and right-oriented Gabors) and asked to press a key continuously according to their current percept. If their percept was a fusion of the two interpretations, they were allowed to press both keys simultaneously.

## Analysis

To compute the survival probabilities in an experiment where observers report continuously their percept, we need to sample the data at regular intervals. For the sake of comparison, we sampled the data with a period of 2 s , starting 1 s after the onset of the stimulus (Figure 17).

It is clear that such a coarse sampling is likely to miss transitory percepts shorter than 2 s , and erroneously mix consecutive identical percepts that are separated by a very short transient. As a result, the mean phase durations will be exaggerated in the sampled version of the continuous data (on average across observers by $15.2 \%$ in our experiment). However, this exaggeration affects all conditions similarly, and is therefore of little concern as long as the experimenter is aware of it. In addition, it is fair to remember that even with continuous data collection, very short phases are likely to be missed because of the observers' unwillingness to press two keys in very fast alternation. Our discrete method of data collection has the advantage of being objective in setting the threshold for the smallest phase analyzed.

## Results

Sampled data were averaged together for the six observers. The survival probabilities look similar to those reported in the other experiments detailed in this manuscript (Figure 18). The asymptotic values are 0.55 and 0.67 for the low- and high-contrast interpretations, respectively.

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Figure 17. Conversion between continuous and discrete sampling. Only the first 60 s of a 5 -min run are shown. Times when the two keys were pressed simultaneously are assigned a percept value of 1.5.


Figure 18. Survival probabilities for the sampled continuous data averaged across observers. The distributions resemble those found with the discreet data collection method discussed in the manuscript.

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